

1. Let $f(x) = x^2 - 3x$

(a) Find R_6 on the interval $[2,5]$. Sketch the graph of $f(x)$ and the corresponding rectangles.

(b) Write the expression for R_n

(c) Write $\int_2^5 f(x) dx$ as the limit of a Riemann sum.

2. Let $f(x) = \begin{cases} \sqrt{4-x^2} & 0 < x < 2 \\ -x + 2 & x \geq 2 \end{cases}$

(a) Sketch the graph of $f(x)$.

(b) Use the graph to evaluate $\int_0^2 f(x) dx$ and $\int_0^3 f(x) dx$

3. Evaluate the following definite integrals:

$$(a) \int_1^4 \left(x^3 - \frac{2}{x} \right) dx \quad Ans: \frac{255}{4} - 4 \ln(2)$$

$$(b) \int_1^4 (3 + x\sqrt{x}) dx \quad Ans: \frac{107}{5}$$

$$(c) \int_{\frac{1}{2}}^{\frac{\sqrt{3}}{2}} \frac{6}{\sqrt{1-t^2}} dt \quad Ans: \pi$$

$$(d) \int_{-1}^0 \frac{1}{1-4x} dx \quad Ans: \frac{\ln(5)}{4}$$

$$(e) \int_0^1 xe^{-x^2} dx \quad Ans: \frac{e-1}{2e}$$

$$(f) \int_0^{\frac{\pi}{2}} \cos x \sin(\sin x) dx \quad Ans: 1 - \cos(1)$$

$$(g) \int_0^1 x\sqrt{1-x} dx \quad (\text{Set } u = 1-x.) \quad Ans: \frac{4}{15}$$

$$(h) \int_0^3 |x^2 - 4| dx \quad (\text{Start by sketching the graph of } f(x) = |x^2 - 4|.) \quad Ans: \frac{23}{3}$$